



8.2 Use Properties of Parallelograms

Goal: Find angle and side measures of parallelograms.

Vocabulary

Polygon: A closed plane figure with 3 or more sides. Each side intersects exactly two other sides at each endpoint.

Quadrilateral: A polygon with four sides whose interior angles sum to 360° .

Diagonal: A segment that joins two non-consecutive vertices of a polygon.

Parallelogram: A quadrilateral with both pairs of opposite sides both parallel and congruent.

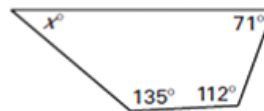
Quadrilateral: A polygon with four sides whose interior angles sum to 360° .

Example 1 Find an unknown interior angle measure

Find the value of x in the diagram shown.

$$135 + 112 + 71 = 318^\circ$$

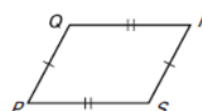
$$360 - 318 = 42^\circ$$



THEOREM 8.3

If a quadrilateral is a parallelogram, then its opposite sides are congruent.

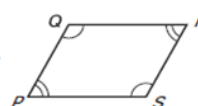
If $PQRS$ is a parallelogram, then $\overline{QP} \cong \overline{RS}$ and $\overline{QR} \cong \overline{PS}$.



THEOREM 8.4

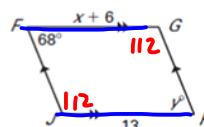
If a quadrilateral is a parallelogram, then its opposite angles are congruent.

If $PQRS$ is a parallelogram, then $\angle P \cong \angle R$ and $\angle Q \cong \angle S$.



Example 2 Use properties of parallelograms

Find the values of x and y .



$$y = 68$$

$$x + 6 = 13$$

$$x = 7$$

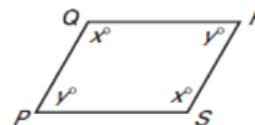
$$\begin{cases} F + H = 68 + 60 = 128 \\ 360 - 128 = 232^\circ = J + G \end{cases}$$

THEOREM 8.5

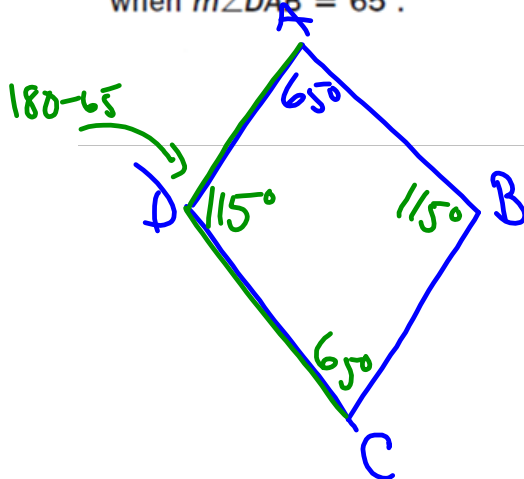
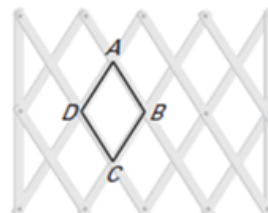
If a quadrilateral is a parallelogram, then its consecutive angles are

Supplementary.

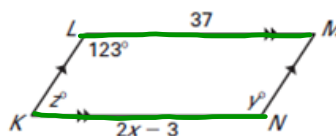
If PQRS is a parallelogram, then $x^\circ + y^\circ = \underline{180^\circ}$.

**Example 3** Use properties of a parallelogram

Gates As shown, a gate contains several parallelograms. Find $m\angle ADC$ when $m\angle DAB = 65^\circ$.



✓ **Checkpoint** Find the indicated measure in $\square KLMN$ shown at the right.



$$y = 123$$

$$z = 57 \quad (180 - 123 = 57)$$

$$2x - 3 = 37$$

$$\begin{array}{r} +3 \quad +3 \\ \hline \end{array}$$

$$2x = 40$$

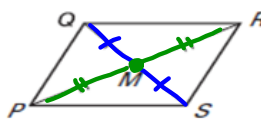
$$\begin{array}{r} \frac{2x}{2} = \frac{40}{2} \\ \hline \end{array}$$

$$x = 20$$

Diagonal: A segment that joins two non-consecutive vertices of a polygon.

THEOREM 8.6

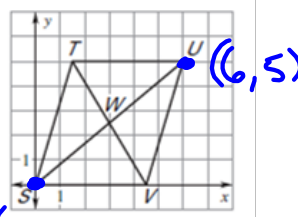
If a quadrilateral is a parallelogram, then its diagonals bisect each other.



$$\overline{QM} \cong \overline{MS} \text{ and } \overline{PM} \cong \overline{MR}$$

Example 4 Use properties of a parallelogram

The diagonals of $\square STUV$ intersect at point W. Find the coordinates of W.

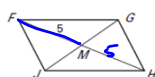


$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

AVERAGE

$$\left(\frac{0+6}{2}, \frac{0+5}{2} \right) = \left(3, \frac{5}{2} \right)$$

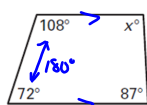
5. Given that $\square FGHI$ is a parallelogram, find MH and FH.



$$MH = 5$$

$$FH = 10$$

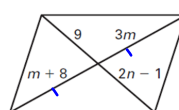
6. Find the value of x.



$$108 + 72 + 87 = 267$$

$$x = 360 - 267 = 93^\circ$$

7. Find the values of m and n.



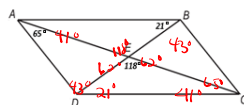
$$m+8 = 3m \quad 2n-1 = 9$$

$$8 = 2m$$

$$4 = m$$

$$2n = 10$$

$$n = 5$$



$$\begin{array}{r} 118 \\ 21 \\ \hline 139 \end{array} \quad \begin{array}{r} 65 \\ 62 \\ \hline 127 \end{array}$$

Find the indicated measure in $\square ABCD$.

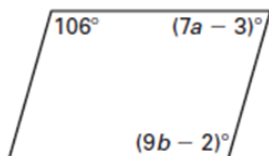
- | | | | |
|-------------------|------|-------------------|------|
| 7. $m\angle AEB$ | 118° | 11. $m\angle BAE$ | 41° |
| 8. $m\angle AED$ | 62° | 12. $m\angle ECB$ | 65° |
| 9. $m\angle BAD$ | 106° | 13. $m\angle DCE$ | 41° |
| 10. $m\angle ADC$ | 64° | 14. $m\angle DCB$ | 106° |

LESSON
8.2**Practice C**

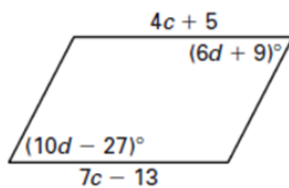
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Find the value of each variable in the parallelogram.

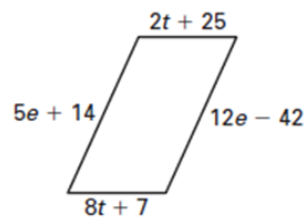
1.



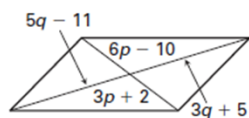
2.



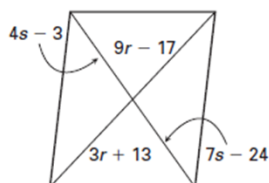
3.



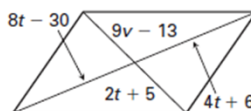
4.



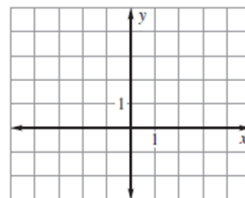
5.



6.



7. The coordinates for $\square ABCD$ are $A(-1, 3)$, $B(4, 2)$, $C(2, -1)$, and $D(-3, 0)$. Plot the points and draw $\square ABCD$ on the coordinate plane. Then draw the diagonals \overline{AC} and \overline{BD} . Label the intersection of the diagonals as point E . What are the coordinates of point E ?



8. In $\square WXYZ$, $m\angle W$ is 50 degrees more than $m\angle X$. Sketch $\square WXYZ$. Find the measure of each interior angle. Then label each angle with its measure.

9. In $\square EFGH$, $m\angle G$ is 25 degrees less than $m\angle H$. Sketch $\square EFGH$. Find the measure of each interior angle. Then label each angle with its measure.

Find the indicated measure in $\square ABCD$.

- | | |
|-------------------|-------------------|
| 10. $m\angle AEB$ | 11. $m\angle BAE$ |
| 12. $m\angle AED$ | 13. $m\angle ECB$ |
| 14. $m\angle BAD$ | 15. $m\angle DCE$ |
| 16. $m\angle ADC$ | 17. $m\angle DCB$ |

