

Class-Notes

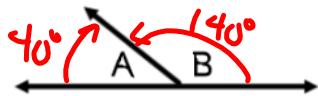
L1 – Proportions, Similarity and Scale Factor

Date \_\_\_\_\_ Period \_\_\_\_\_

**Ratio:** A comparison of two numbers.

$$\frac{a}{b} \quad \text{OR} \quad a:b$$

Ex 1: Find the ratio of  $\angle A$  to  $\angle B$  in the linear pair if  $m\angle B = 140^\circ$ .

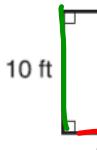


$$\frac{m\angle A}{m\angle B} = \frac{40}{140} \div 10 = \frac{4}{14} = \frac{2}{7}$$

**Proportion:** An equation that sets two ratios equal.

Ex 2: Write a proportion for the corresponding sides of the rectangles below.

$$\frac{2}{2} = 1$$



**SMALL** : **LARGE**

$$\frac{10\text{ft}}{15\text{ft}} = \frac{8\text{ft}}{12\text{ft}}$$

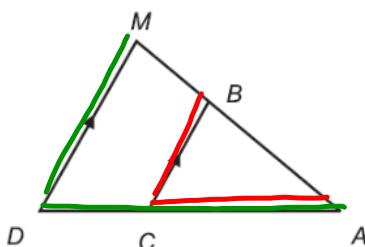
$$\frac{2}{3} = \frac{2}{3}$$

$$\frac{\text{ft}}{\text{ft}} = 1$$

Ex 3: Complete each proportion.

$\triangle ABC$

$\triangle ABD$



$$\frac{AB}{BM} = \frac{AC}{CD}$$

$$\frac{AD}{AC} = \frac{AB}{BM}$$

$$\frac{CB}{DM} = \frac{AC}{AD}$$

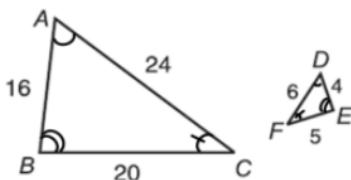
**Scale Factor:** The ratio of lengths of two corresponding sides of similar figures.

Ex 4: Give the scale factor of the small rectangle to the big rectangle in example 2.

SCALE FACTOR IS  $\frac{2}{3}$  or  $2:3$   $\rightsquigarrow 1:1.5$

**Similar Figures:** Two figures that have all corresponding angles congruent and all corresponding sides proportional.

Ex 5: A) List all of the corresponding angles for the triangles below. Then list the corresponding sides in a proportion.



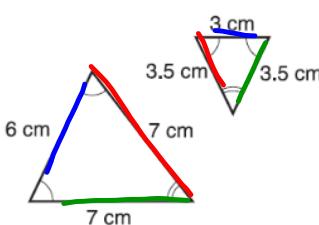
$$\begin{aligned} \angle A &\cong \angle D \\ \angle B &\cong \angle E \\ \angle C &\cong \angle F \end{aligned}$$

$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$$

B) Write a similarity statement for the triangles above. Then give the scale factor for the triangles.

"IS SIMILAR TO"  
 $\triangle ABC \sim \triangle DEF$

Ex 6: Determine if the polygons are similar. Justify your answer.



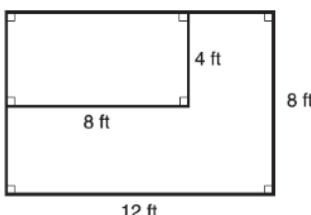
$$\frac{7 \times 2}{3.5 \times 2} = \frac{7}{3.5} = \frac{6}{3}$$

$$\frac{14}{7} = \frac{14}{7} = \frac{2}{1}$$

$$\boxed{\frac{2}{1} = \frac{2}{1} = \frac{2}{1}}$$

YES : ALL RATIOS ARE EQUAL

Ex 7: Determine if the polygons are similar. Justify your answer.

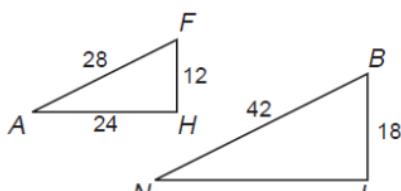


$$\frac{4}{8} = \frac{8}{12}$$

$S : L$

NOT SIMILAR:  
 $\frac{1}{2} \neq \frac{2}{3}$  RATIOS  $\neq$

Ex 8: Determine the scale factor of  $\triangle FHA$  to  $\triangle BLN$  and of  $\triangle BLN$  to  $\triangle FHA$ .



$$\frac{\triangle FHA}{\triangle BLN} \rightarrow \frac{28}{42} = \frac{24}{36} = \frac{12}{18}$$

$$\frac{4}{6} = \frac{4}{6} = \frac{2}{3}$$

SF.  $\triangle FHA$  to  $\triangle BLN$  is  $\frac{2}{3}$  or 2:3

$\triangle BLN$  to  $\triangle FHA$  is  $\frac{3}{2}$  or 3:2

$$\boxed{\frac{2}{3} = \frac{2}{3} = \frac{2}{3}}$$