

## Solving "Basic" Trigonometric Equations

Students will be able to solve trigonometric equations.

## Honors Precalculus

What steps are needed to solve Trig equations?

Use Algebra techniques to isolate the Trig function:

- Add/Subtract/Multiply/Divide both sides
  - By NUMBERS; NOT trig functions
- Factor
- Use the quadratic formula
  - $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
- Square root both sides
- ETC.

Then: Use an inverse trig function ( $\sin^{-1}$ ;  $\cos^{-1}$ ;  $\tan^{-1}$ ) to solve for the angle(s)

(Or recognize values of trig functions from the Unit Circle)

- Often times there are many angles that are solutions ☺

### Example 1:

Solve  $2\sin x = 1$  for all angle values of  $x$  on the interval  $[0, 2\pi]$

$$\begin{aligned} 2\sin x &= 1 \\ \sin x &= \frac{1}{2} \end{aligned}$$

$x = \frac{\pi}{6}, \frac{5\pi}{6}$   
 $30^\circ, 150^\circ$

### Example 2:

Solve  $\cos 2x + \sqrt{3} = -\cos 2x$  for all angle values of  $x$  on the interval  $[0, 2\pi]$

$$\begin{aligned} \cos 2x + \sqrt{3} &= -\cos 2x \\ +\cos 2x & \\ \hline 2\cos 2x + \sqrt{3} &= 0 \\ 2\cos 2x &= -\sqrt{3} \\ \cos 2x &= -\frac{\sqrt{3}}{2} \end{aligned}$$

$2x = \frac{5\pi}{6}$        $x = \frac{5\pi}{12}$   
 $(150^\circ)$        $(75^\circ)$   
 $2x = \frac{7\pi}{6}$        $x = \frac{7\pi}{12}$   
 $(210^\circ)$        $(105^\circ)$

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Example 3: Solve  $3\cot^2 x - 1 = 0$  for all values of  $x$

$$3\cot^2 x - 1 = 0$$

$$3\cot^2 x = 1$$

$$\cot^2 x = \frac{1}{3}$$

$$\cot x = \pm \frac{1}{\sqrt{3}}$$

$$\tan x = \pm \sqrt{3}$$

$$x = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3} \} + 2n\pi$$

Example 4:

Solve  $2\sin^2 x - \sin x - 1 = 0$  for all values of  $x$

$$2a^2 - a - 1 \quad \text{if } a = \sin x$$

$$(2\sin x + 1)(\sin x - 1) = 0 \quad (2a + 1)(a - 1) = 0$$

$$2\sin x + 1 = 0$$

$$2\sin x = -1$$

$$\sin x = -\frac{1}{2}$$

$$x = \frac{7\pi}{6}, \frac{11\pi}{6} \} + 2n\pi$$

$$\sin x - 1 = 0$$

$$\sin x = 1$$

$$x = \frac{\pi}{2} + 2n\pi$$

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### Example 5:

Solve  $\sqrt{2}\csc x + 2 = 4$  for all values of  $x$

$$\sqrt{2}\csc x = 2$$

so...  $\csc x = \frac{2}{\sqrt{2}}$

$$\sin x = \frac{\sqrt{2}}{2}$$

$$x = \frac{\pi}{4}, \frac{3\pi}{4} \} + 2n\pi$$

### Example 6:

Solve  $\sec^2 x = \frac{4}{3}$  for all values of  $x$

so  $\sec x = \frac{2}{\sqrt{3}}$

$$\cos x = \frac{\sqrt{3}}{2}$$

$$x = \frac{\pi}{6}, \frac{7\pi}{6} \} + 2n\pi$$