

Solving Rational Equations; Practice

Name \_\_\_\_\_

Solve the rational equations. State the excluded values for the variable (What it can not equal).

(y+3).  $\frac{5}{y+3} - 2 = \frac{7}{y+3}$

What can y not equal? 3

$$\begin{aligned} 5 - 2(y+3) &= 7 \\ 5 - 2y + 6 &= 7 \\ -2y &= 8 \\ \boxed{y = -4} \end{aligned}$$

(a-2).  $\frac{8}{a-2} + 5 = \frac{4a}{a-2}$

What can a not equal? 2

$$\begin{aligned} 8 + 5(a-2) &= 4a && \text{NO SOLUTION} \\ 8 + 5a - 10 &= 4a \\ \boxed{a = 2} \end{aligned}$$

(x+7).  $\frac{5}{x+7} + 1 = \frac{4}{x+7}$

What can x not equal? -7

$$\begin{aligned} 5 + x + 7 &= 4 \\ 5 + x &= -3 \\ \boxed{x = -8} \end{aligned}$$

(x-5).  $\frac{5}{x-5} = 2 - \frac{x-3}{x-5}$

What can x not equal? 5

$$\begin{aligned} 5 &= 2(x-5) - (x-3) \\ 5 &= 2x - 10 - x + 3 \\ 5 &= x - 7 \\ \boxed{12 = x} \end{aligned}$$

(k+1)(k-2).  $\frac{k}{k+1} = \frac{3}{k^2-k-2} - \frac{k}{k-2}$

What can k not equal? -1, 2

$$\begin{aligned} k(k-2) &= 3 - k(k+1) \\ k^2 - 2k &= 3 - k^2 - k \\ 2k^2 - k - 3 &= 0 \\ (2k-3)(k+1) &= 0 \\ \boxed{k = \frac{3}{2}} \quad \cancel{k = -1} \end{aligned}$$

(x^2-4).  $\frac{10}{x^2-4} = 1 - \frac{1}{x+2}$

What can x not equal? -2

$$\begin{aligned} 10 &= x^2 - 4 - (x-2) \\ 10 &= x^2 - 4 - x + 2 \\ 10 &= x^2 - x - 2 \\ 0 &= x^2 - x - 12 \\ 0 &= (x-4)(x+3) \\ \boxed{x = 4} \quad \boxed{x = -3} \end{aligned}$$

$$7. \left( \frac{25}{x} = 10 - x \right) \times \quad \text{What can } x \text{ not equal?}$$

$$25 = 10x - x^2$$

$$x^2 - 10x + 25 = 0$$

$$(x-5)^2 = 0$$

$$x = 5$$

$$8. \left( \frac{2n-3}{2} = \frac{3^2}{4} + \frac{n-4}{8} \right) \text{What can } n \text{ not equal?}$$

$$4(2n-3) = 6 + n - 4$$

$$8n - 12 = 6 + n - 4$$

$$8n - 12 = n + 2$$

$$7n = 14$$

$$n = 2$$

NO  
RESTRICTIONS

$$9. \frac{13}{x^2-9} + \frac{3}{3-x} = \frac{2}{x+3} \quad \text{What can } x \text{ not equal?}$$

$$13 - 3(x+3) = 2(x-3)$$

$$13 - 3x - 9 = 2x - 6$$

$$-3x + 4 = 2x - 6$$

$$10 = 5x$$

$$2 = x$$

$$10. \left( \frac{x-3}{2} = \frac{1}{x-4} \right) \text{What can } x \text{ not equal?}$$

$$(x-3)(x-4) = 1(2)$$

$$x^2 - 7x + 12 = 2$$

$$x^2 - 7x + 10 = 0$$

$$(x-5)(x-2)$$

$$x = 5, x = 2$$

$$11. \left( \frac{2m-1}{3m+1} = \frac{m-1}{m+1} \right) \text{What can } m \text{ not equal?}$$

$$(2m-1)(m+1) = (3m+1)(m-1)$$

$$2m^2 + m - 1 = 3m^2 - 2m - 1$$

$$0 = m^2 - 3m$$

$$0 = m(m-3)$$

$$m = 0 \quad m = 3$$

$$12. \left( \frac{y+5}{y-4} - \frac{5}{y-2} = \frac{7y-4}{y^2-6y+8} \right) \text{What can } y \text{ not equal?}$$

$$(y+5)(y-2) - 5(y-4) = 7y-4$$

$$y^2 + 3y - 10 - 5y + 20 = 7y - 4$$

$$y^2 - 2y + 10 = 7y - 4$$

$$y^2 - 9y + 14 = 0$$

$$(y-7)(y-2) = 0$$

$$y = 7, y = 2$$